



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.OA.1

Interpret a multiplication equation as a comparison, e.g., interpret $35 = 5 \times 7$ as a statement that 35 is 5 times as many as 7 and 7 times as many as 5. Represent

verbal statements of multiplicative comparisons as multiplication equations.

Essential Understandings

- Comparisons can be additive or multiplicative depending on the mathematical situation.
- In multiplicative comparisons, the relationship between quantities is described in terms of how many times larger one is than the other

Common Misconceptions

Key words are misleading. Some key words typically mean addition or subtraction. But not always.

Consider: There were 4 jackets left on the playground on Monday and 5 jackets left on the playground on Tuesday. How many jackets were left on the playground? "Left" in this problem does not mean subtract.

Many problems have no key words. For example, How many legs do 7 elephants have?, does not have a key word. However, students should be able to solve the problem by thinking and drawing a picture or building a model.

It sends a bad message. The most important strategy when solving a problem is to make sense of the problem and to think. Key words encourage students to ignore meaning and look for a formula. Mathematics is about meaning (Van de Walle, 2012).

Academic Vocabulary/ Language

- multiplication
- equation
- multiplicative

Tier 2

- interpret
- represent
- comparison

Learning Targets

I can explain how one factor in a multiplication problem changes the other factor to make the product.
I can write verbal statements about multiplicative comparisons as equations.

Classroom Snapshot

Example

35 is 5 times bigger than 7 AND 35 is 7 times bigger than 5.
Explain how the expression $3 \times 7 = 21$ tells you how many times larger 21 is than 3.

Adapted from Darke County Schools

Questions

Write an expression that shows how much bigger 24 is than 8.
($24 = 3 \times 8$)

John says that he is thinking of a number that is 7 times bigger than 3.
Write an equation to express the relationship.

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Students need to solve word problems involving multiplicative comparison (product unknown, partition unknown) using multiplication or division as shown in Table 2 of the Ohio New Learning Standards for Mathematics, page 89. <http://www.corestandards.org/Math/>
They should use drawings or equations with a symbol for the unknown number to represent the problem. Students need to be able to distinguish whether a word problem involves multiplicative comparison or additive comparison (solved when adding and subtracting in Grades 1 and 2).

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Know relative sizes of measurement units within one system of units (4.MD.1).

Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money (4.MD.2)

3.OA.3 & 8 (Prior Grade Standard)

3. Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

8. Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.

5.OA.2 (Future Grade Standard)

Write simple expressions that record calculations with numbers, and interpret numerical expressions without evaluating them.



COLUMBUS CITY SCHOOLS

Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.OA.2

Multiply or divide to solve word problems involving multiplicative comparison, e.g., by using drawings and equations with a symbol for the unknown number to represent the

problem, distinguishing multiplicative comparison from additive comparison. See Table 2, page 96. Drawings need not show details, but should show the mathematics in the problem. (This applies wherever drawings are mentioned in the Standards.)

Essential Understanding

- Comparisons can be additive or multiplicative depending on the mathematical situation.
- In multiplicative comparisons, the relationship between quantities is described in terms of how many times larger one is than the other.

Common Misconceptions

Key words are misleading. Some key words typically mean addition or subtraction. But not always. Consider: There were 4 jackets left on the playground on Monday and 5 jackets left on the playground on Tuesday. How many jackets were left on the playground? "Left" in this problem does not mean subtract.

Many problems have no key words. For example, How many legs do 7 elephants have?, does not have a key word. However, most students should be able to solve the problem by thinking and drawing a picture or building a model. **It sends a bad message.** The most important strategy when solving a problem is to make sense of the problem and to think. Key words encourage students to ignore meaning and look for a formula. Mathematics is about meaning (Van de Walle, 2012).

Academic Vocabulary/ Language

- multiplication
- equation
- multiplicative
- symbol for unknown

Tier 2

- solve
- comparison
- distinguish

Learning Targets

- I can solve real world problems that require me to multiply and divide whole numbers.
- I can solve word problems involving multiplication and division by using drawings.
- I can solve word problems involving multiplication and division by using equations and a symbol for an unknown.
- I can explain the difference between a multiplicative comparison and an additive comparison.

Classroom Snapshot

Examples

Draw a picture showing how to share 17 cookies among 5 friends.

Sara says that she is 4 times older than her baby brother. If Sara is 12 years old, how old is her baby brother. Explain how we could use the equation $4 \times B = 12$ to solve this problem.

Adapted from Darke County Schools

Questions

If Mary is 11 and her sister is 22, explain how her sister is 11 years older OR 2 times older.

Mrs. March is buying pencils for her classroom. She bought 6 packs of green pencils and 4 packs of pink pencils. There are 10 green pencils in each pack and 12 pink pencils in each pack. What is the total number of pencils Mrs. Marsh bought for her classroom?

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Students need to solve word problems involving multiplicative comparison (product unknown, partition unknown) using multiplication or division as shown in Table 2 of the Ohio New Learning Standards for Mathematics, page 89. <http://www.corestandards.org/Math/>

They should use drawings or equations with a symbol for the unknown number to represent the problem. Students need to be able to distinguish whether a word problem involves multiplicative comparison or additive comparison (solved when adding and subtracting in Grades 1 and 2).

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

TABLE 2. COMMON MULTIPLICATION AND DIVISION SITUATIONS¹

	UNKNOWN PRODUCT $3 \times 6 = ?$	GROUP SIZE UNKNOWN (“HOW MANY IN EACH GROUP?” DIVISION) $3 \times ? = 18$, AND $18 \div 3 = ?$	NUMBER OF GROUPS UNKNOWN (“HOW MANY GROUPS?” DIVISION) $? \times 6 = 18$, AND $18 \div 6 = ?$
EQUAL GROUPS	<p>There are 3 bags with 6 plums in each bag. How many plums are there in all?</p> <p>Measurement example. You need 3 lengths of string, each 6 inches long. How much string will you need altogether?</p>	<p>If 18 plums are shared equally into 3 bags, then how many plums will be in each bag?</p> <p>Measurement example. You have 18 inches of string, which you will cut into 3 equal pieces. How long will each piece of string be?</p>	<p>If 18 plums are to be packed 6 to a bag, then how many bags are needed?</p> <p>Measurement example. You have 18 inches of string, which you will cut into pieces that are 6 inches long. How many pieces of string will you have?</p>
ARRAYS², AREA³	<p>There are 3 rows of apples with 6 apples in each row. How many apples are there?</p> <p>Area example. What is the area of a 3 cm by 6 cm rectangle?</p>	<p>If 18 apples are arranged into 3 equal rows, how many apples will be in each row?</p> <p>Area example. A rectangle has area 18 square centimeters. If one side is 3 cm long, how long is a side next to it?</p>	<p>If 18 apples are arranged into equal rows of 6 apples, how many rows will there be?</p> <p>Area example. A rectangle has area 18 square centimeters. If one side is 6 cm long, how long is a side next to it?</p>
COMPARE	<p>A blue hat costs \$6. A red hat costs 3 times as much as the blue hat. How much does the red hat cost?</p> <p>Measurement example. A rubber band is 6 cm long. How long will the rubber band be when it is stretched to be 3 times as long?</p>	<p>A red hat costs \$18 and that is 3 times as much as a blue hat costs. How much does a blue hat cost?</p> <p>Measurement example. A rubber band is stretched to be 18 cm long and that is 3 times as long as it was at first. How long was the rubber band at first?</p>	<p>A red hat costs \$18 and a blue hat costs \$6. How many times as much does the red hat cost as the blue hat?</p> <p>Measurement example. A rubber band was 6 cm long at first. Now it is stretched to be 18 cm long. How many times as long is the rubber band now as it was at first?</p>
GENERAL	$a \times b = ?$	$a \times ? = p$, and $p \div a = ?$	$? \times b = p$, and $p \div b = ?$

Connections Across Standards

Know relative sizes of measurement units within one system of units (4.MD.1).

Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money (4.MD.2).

3.OA.3 & 8 (Prior Grade Standard)

3. Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

8. Solve two-step word problems using the four operations. Represent

5.OA.2 (Future Grade Standard)

Write simple expressions that record calculations with numbers, and interpret numerical expressions without evaluating them.

these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.	
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Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

<div style="border: 1px solid black; border-radius: 15px; padding: 10px; display: inline-block; margin-bottom: 10px;"> 4.OA.3 </div> <p>Solve multistep word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.</p>	<p>Solve multistep word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.</p>	<p>Common Misconceptions Students have difficulty estimating a two-step problem. Students do not always solve all of the steps needed for a multistep problem. Students may not be able to identify which part of the equation is unknown in order to represent it as a variable. Students may not know how to interpret a remainder.</p>	<p>Academic Vocabulary/ Language</p> <ul style="list-style-type: none"> ▪ operations ▪ equations ▪ mental computation ▪ estimation ▪ rounding ▪ remainder ▪ unknown quantity ▪ multistep <p>Tier 2</p> <ul style="list-style-type: none"> ▪ reasonableness ▪ represent
<p style="text-align: center;">Essential Understandings</p> <ul style="list-style-type: none"> ● Use the four operations with whole numbers to solve problems. ● Estimation strategies, including rounding, can be used to determine the reasonableness of answers. ● An unknown can be in any position of a multiplicative comparison problem. 			
<p>Learning Targets</p>	<p>I can solve real world problems that require me to add, subtract, multiply, divide whole numbers. I can solve multi-step word problems using addition, subtraction, multiplication and division with remainders. I can solve multi-step word problems using addition, subtraction, multiplication and division using equations where a symbol is used for the unknown. I can determine if the answer makes sense by using mental math, estimation, and rounding.</p>		

Classroom Snapshot

Examples

Explain how Jack could estimate how much he needs in order to buy 32 pieces of candy at 19 cents each.

Explain how Pedro might estimate how much money he needs to buy 4 items that cost \$4.12, \$2.51, \$7.99 and \$1.48.

Questions

There are 17 members on three teams. How many vans will be necessary to carry them if each van carries 11 people?

Lucy's room has an area of 165 sq. ft. Write an equation to find the length of Lucy's room if the width is 11 feet. Solve to find the length.

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Present multi-step word problems with whole numbers and whole-number answers using the four operations. Students should know which operations are needed to solve the problem. Drawing pictures or using models will help students understand what the problem is asking. They should check the reasonableness of their answer using mental computation and estimation strategies.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Know relative sizes of measurement units within one system of units (4.MD.1).

Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money (4.MD.2).

3.OA.3 & 8 (Prior Grade Standard)

3. Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

8. Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.

5.OA.1 (Future Grade Standard)

Use parentheses, brackets, or braces in numerical expressions, and evaluate expressions with these symbols.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.OA.4

Find all factor pairs for a whole number in the range 1–100. Recognize that a whole number is a multiple of each of its factors. Determine whether a given whole number in the range 1–100 is a multiple of a given one-digit number. Determine whether a given whole number in the range 1–100 is prime or composite.

Essential Understandings

- A number can be multiplicatively decomposed into factor pairs and expressed as a product of these factor pairs.
- A prime number has only two factors: one and itself (only one factor pair).
- A composite number has more than two factors (more than one factor pair).
- Any whole number is a multiple of each of its factors.

Common Misconceptions

When listing multiples of numbers, students may not list the number itself. Emphasize that the smallest multiple is the number itself.

Some students may think that larger numbers have more factors. Having students share all factor pairs and how they found them will clear up this misconception.

Academic Vocabulary/ Language

- factor
- product
- multiples
- odd/even numbers
- prime
- composite

Tier 2

- recognize
- determine
- explain
- show
- find

Learning Targets

- I can find all factor pairs for a whole number between 1 and 100.
- I can show how a whole number is a multiple of each of its factors.
- I can determine if a whole number between 1 and 100 is a multiple of a particular one digit number.
- I can determine the numbers between 1-100 that are prime or composite.

Classroom Snapshot

Examples

Jasmine says that all odd numbers are prime numbers. Devon says that Jasmine is wrong because 9 is odd but 9 is also composite. Who is right? Why?

Giovanni listed the factors for 12 as 1, 2, 3, 4, 6, 12. Is he correct? How do you know?

Adapted from Darke County Schools

Questions

Explain how to find all the single digit factors of 24.

Name 3 numbers between 40 and 50 that have no other factors than one and itself.

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Students need to develop strategies for determining if a number is prime or composite, in other words, if a number has a whole number factor that is not one or itself. Starting with a number chart of 1 to 20, use multiples of prime numbers to eliminate later numbers in the chart. For example, 2 is prime but 4, 6, 8, 10, 12, ... are composite. Encourage the development of rules that can be used to aid in the determination of composite numbers. For example, other than 2, if a number ends in an even number (0, 2, 4, 6 and 8), it is a composite number.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Use multiplication and division with whole numbers to solve problems and make multiplicative comparisons (4.OA.1-2).

3.OA.1 (Prior Grade Standard)

Interpret products of whole numbers, e.g., interpret 5×7 as the total number of objects in 5 groups of 7 objects each.

(Future Grade Standard)

N/A



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.OA.5

Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself.

For example, given the rule "Add 3" and the starting number 1 generate terms in the resulting sequence and observe that the terms appear to alternate between odd and even numbers. Explain informally why the numbers will continue to alternate in this way.

Essential Understanding

- Explore patterns that consist of repeated sequences of shapes.
- Explore patterns that consist of growing sequences of designs.
- Explore patterns that consist of repeatedly adding the same whole number or repeatedly multiplying by the same whole number.
- Identify features of given or generated patterns.
- Make and describe generalizations about patterns.
- Connect rules and terms of patterns to numerical concepts.

Common Misconceptions

Students may assume all patterns have the same rule due to limited exposure. This standard is the first formal approach to patterns. Students should have ample opportunities working with and creating patterns.

Academic Vocabulary/ Language

- number pattern
- shape pattern

Tier 2

- generate
- identify
- apparent
- features
- explicit
- rule
- analyze

Learning Targets

- I can generate a number pattern that follows a given rule.
- I can generate a shape pattern that follows a given rule.
- I can look at a number pattern and determine additional patterns found within the sequence.
- I can look at a shape pattern and determine additional patterns found within the sequence.

Classroom Snapshot

Examples

Generate the next 5 numbers in the number pattern that follows the rule “half as big” and starts with 12.

If a number pattern is created by the rule “add three”, will there be more odd numbers or even numbers created?

Questions

Look at the following pattern. What is the rule for this pattern? What number comes next?

7, 14, 21, 28, _____

What comes next in this pattern?



Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

In order for students to be successful later in the formal study of algebra, their algebraic thinking needs to be developed. Understanding patterns is fundamental to algebraic thinking. Students have experience in identifying arithmetic patterns, especially those included in addition and multiplication tables. Contexts familiar to students are helpful in developing students’ algebraic thinking. Students should generate numerical or geometric patterns that follow a given rule. They should look for relationships in the patterns and be able to describe and make generalizations.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Extend the understanding of fraction equivalence (4.NF.1- 2).

3.OA.9 (Prior Grade Standard)

Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations. For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.

5.NBT.2 and 5.OA.3 (Future Grade Standard)

NBT.2 Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole number exponents to denote powers of 10. OA.3 Generate two numerical patterns using two given rules. Identify apparent relationships between corresponding terms. Form ordered pairs consisting of corresponding terms from the two patterns, and graph the ordered pairs on a coordinate plane. For example, given the rule “Add 3” and the starting number 0, and given the rule “Add 6” and the starting number 0, generate terms in the resulting sequences, and observe that the terms in one sequence are twice the corresponding terms in the other sequence. Explain informally why this is so.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.NBT.1

Recognize that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right by applying concepts of place value, multiplication, or division.

Essential Understandings

- Generalize place value understanding for multi-digit whole numbers less than or equal to 1,000,000.
- In the base-ten system, the value of each place is 10 times the value of the place to the immediate right.

Common Misconceptions

Students may have misconceptions about writing numerals from verbal descriptions. Numbers like one thousand do not cause a problem; however a number like one thousand two causes problems for students. Many students will understand the 1000 and the 2 but then instead of placing the 2 in the ones place, students will write the numbers as they hear them, 10002 (ten thousand two). Students often assume that the first digit of a multi-digit number indicates the "greatness" of a number. The assumption is made that 954 is greater than 1002 because students are focusing on the first digit instead of the number as a whole. Students need to be aware of the greatest place value.

Academic Vocabulary/Language

- place value
- digit

Tier 2

- recognize
- represents
- apply
- concept

Learning Targets	<p>I can use and explain place value concepts for multi-digit whole numbers.</p> <p>I can look at a multi-digit number and determine that the digit to the left is 10 times greater than a given digit.</p> <p>I can use place value to help multiply or divide numbers.</p>
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Classroom Snapshot

Examples

Explain why $700 \div 7 = 100$ without actually computing the problem.

Explain why each column in a multi-digit number increases by 10 times.

Questions

What must you multiply 6 by to get the number 60?
To get to 600?

Describe the size difference between 120 and 12.

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Students also need to create numbers that meet specific criteria. For example, provide students with cards numbered 0 through 9. Ask students to select 4 to 6 cards; then, using all the cards make the largest number possible with the cards, the smallest number possible and the closest number to 5000 that is greater than 5000 or less than 5000.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Solve multi-step word problems with whole numbers and assess the reasonableness of answers using mental computation and estimation strategies (4.OA.3).

Solve problems involving metric measurement and conversions from a larger unit to a smaller unit (4.MD.1-2).

3.NBT.3 (Prior Grade Standard)

Multiply one-digit whole numbers by multiples of 10 in the range 10-90, e.g., 9×80 , 5×60 using strategies based on place value and properties of operations.

5.NBT.1 (Future Grade Standard)

Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and 1/10 of what it represents in the place to its left



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.NBT.2

Read and write multi-digit whole numbers using standard form, word form, and expanded form.^G Compare two multi-digit numbers based on meanings of the digits in each place, using $>$, $=$, and $<$ symbols to record the results of comparisons. Grade 4 expectations in this domain are limited to whole numbers less than or equal to 1,000,000.

Essential Understandings

- Generalize place value understanding for multi-digit whole numbers less than or equal to 1,000,000.
- Numbers can be expressed in standard form, word form, and expanded form.

Common Misconceptions

Students may have misconceptions about writing numerals from verbal descriptions. Numbers like one thousand do not cause a problem; however a number like one thousand two causes problems for students. Many students will understand the 1000 and the 2 but then instead of placing the 2 in the ones place, students will write the numbers as they hear them, 10002 (ten thousand two). There are multiple strategies that can be used to assist with this concept, including place-value boxes and vertical-addition method. Students often assume that the first digit of a multi-digit number indicates the "greatness" of a number. The assumption is made that 954 is greater than 1002 because students are focusing on the first digit instead of the number as a whole. Students need to be aware of the greatest place value.

Academic Vocabulary/ Language

- place value
- digit
- expanded form
- written form
- word form
- greater than ($>$)
- less than ($<$)
- equal to ($=$)
- multi-digit

Tier 2

- compare
- explain

Learning Targets

I can use and explain place value concepts for multi-digit whole numbers.
 I can read and write multi-digit whole numbers using word form, expanded form and word form.
 I can compare the size of two multi-digit numbers using place value and record the results with $<$, $>$, $=$.

Classroom Snapshot

Examples

Write the word form for 307.

Write five thousand thirty two in number form.

Explain why 811 is greater than 799 and write an expression using $<$ or $>$.

Questions

Write the number that represents two hundreds and seven ones.

Write the number that is represented by the expanded form $14,000 + 80 + 6$.

Write an inequality comparing 813 and 831.

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Provide multiple opportunities in the classroom setting and use real-world context for students to read and write multi-digit whole numbers. Students need to have opportunities to compare numbers with the same number of digits, e.g., compare 453, 698 and 215; numbers that have the same number in the leading digit position, e.g., compare 45, 495 and 41,223; and numbers that have different numbers of digits and different leading digits, e.g., compare 312, 95, 5245 and 10,002.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Solve multi-step word problems with whole numbers and assess the reasonableness of answers using mental computation and estimation strategies (4.OA.3).

Solve problems involving metric measurement and conversions from a larger unit to a smaller unit (4.MD.1-2).

(Prior Grade Standard)

N/A

5.NBT.3a (Future Grade Standard)

Read, write, and compare decimals to thousandths.

a. Read and write decimals to thousandths using base-ten numerals, number names, and expanded form^G, e.g., $347.392 = 3 \times 100 + 4 \times 10 + 7 \times 1 + 3 \times (1/10) + 9 \times (1/100) + 2 \times (1/1000)$.

b. Compare two decimals to thousandths based on meanings of the digits in each place, using $>$, $=$, and $<$ symbols to record the results of comparisons.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

<div style="border: 1px solid black; border-radius: 15px; padding: 10px; display: inline-block;"> <h3 style="margin: 0;">4.NBT.3</h3> </div>	<p>Use place value understanding to round multi-digit whole numbers to any place through 1,000,000.</p>	<p>Common Misconceptions</p>	<p>Academic Vocabulary/ Language</p>
<p>Essential Understandings</p> <ul style="list-style-type: none"> • Generalize place value understanding for multi-digit whole numbers less than or equal to 1,000,000. • Rounding helps solve problems mentally and assess the reasonableness of an answer. 		<p>There are several misconceptions students may have about writing numerals from verbal descriptions. Numbers like one thousand do not cause a problem; however a number like one thousand two causes problems for students. Many students will understand the 1000 and the 2 but then instead of placing the 2 in the ones place, students will write the numbers as they hear them, 10002 (ten thousand two). There are multiple strategies that can be used to assist with this concept, including place-value boxes and vertical -addition method. Students often assume that the first digit of a multi-digit number indicates the "greatness" of a number. The assumption is made that 954 is greater than 1002 because students are focusing on the first digit instead of the number as a whole. Students need to be aware of the greatest place value.</p>	<ul style="list-style-type: none"> • place value • digit • multi-digit • rounding • whole numbers <p style="text-align: center;">Tier 2</p> <ul style="list-style-type: none"> • explain
<p>Learning Targets</p>	<p>I can use and explain place value concepts for multi-digit whole numbers. I can round whole numbers to the nearest 10, 100, 1000,</p>		

Classroom Snapshot

Example

The number 2,341 is between what two “hundreds numbers”?

Explain why 997 and 1,435 both round to 1000 as the nearest 1000.

Question

Jerry says that 6,450 rounds to 6,400 and Jill says that it rounds to 6,500. Who is correct? Explain your thinking.

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

In Grade 4, rounding is not new, and students need to build on the Grade 3 skill of rounding to the nearest 10 or 100 to include larger numbers and place value. What is new for Grade 4 is rounding to digits other than the leading digit, e.g., round 23,960 to the nearest hundred. This requires greater sophistication than rounding to the nearest ten thousand because the digit in the hundreds place represents 900 and when rounded it becomes 1000, not just zero. Students should also begin to develop some rules for rounding, building off the basic strategy of, “Is 48 closer to 40 or 50?” Since 48 is only 2 away from 50 and 8 away from 40, 48 would round to 50. Now students need to generalize the rule for much larger numbers and rounding to values that are not the leading digit.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Solve multi-step word problems with whole numbers and assess the reasonableness of answers using mental computation and estimation strategies (4.OA.3).

Solve problems involving metric measurement and conversions from a larger unit to a smaller unit (4.MD.1-2).

3.NBT.1(Prior Grade Standard)

Use place value understanding to round whole numbers to the nearest 10 or 100.

5.NBT.4 (Future Grade Standard)

Use place value understanding to round decimals to any place, millions through hundredths.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

<p>4.NBT.4</p>	<p>Fluently ^G add and subtract multi-digit whole numbers using a standard algorithm ^G.</p>	<p>Common Misconceptions Often students mix up when to 'carry' and when to 'borrow'. Also students often do not understand why they need to regroup and just subtract the smaller digit from the larger one. Emphasize place value and the meaning of each of the digits.</p>	<p>Academic Vocabulary/ Language</p> <ul style="list-style-type: none"> • add • subtract • algorithm ▪ multi-digit <p>Tier 2</p> <ul style="list-style-type: none"> • fluently ▪ arithmetic
<p>Essential Understandings</p> <ul style="list-style-type: none"> • There are different algorithms that can be used to add or subtract. • Fluency is being efficient, accurate, and flexible with strategies. 			
<p>Learning Targets</p>	<p>I can use and explain how to do arithmetic with multi-digit numbers. I am FLUENT with addition and subtraction. I can easily and accurately add and subtract multi-digit whole numbers.</p>		

Classroom Snapshot

Example

$$513 - 248 = ?$$

The library loaned out 348 books on Monday, 425 books on Tuesday and 612 books on Wednesdays. How many books did the library loan out during those three days in all? Explain.

Adapted from Darke County Schools

Question

$$\text{Solve: } 389 + 267 - 499$$

Mrs. Allen bought a package of 1000 stickers. She gave away 430 stickers during the first half of the school year. How many stickers does Mrs. Allen have left? Explain.

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

A crucial theme in multi-digit arithmetic is encouraging students to develop strategies that they understand, can explain, and can think about, rather than merely follow a sequence of directions that they don't understand. It is important for students to have seen and used a variety of strategies and materials to broaden and deepen their understanding of place value before they are required to use standard algorithms. The goal is for them to understand all the steps in the algorithm, and they should be able to explain the meaning of each digit. For example, a 1 can represent one, ten, one hundred, and so on. For multi-digit addition and subtraction in Grade 4, the goal is also fluency, which means students must be able to carry out the calculations efficiently and accurately. Start with a student's understanding of a certain strategy, and then make intentional, clear-cut connections for the student to the standard algorithm. This allows the student to gain understanding of the algorithm rather than just memorize certain steps to follow.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Multiply or divide to solve word problems involving multiplicative comparisons (4.OA.2).

Solve multi-step word problems with whole numbers and assess the reasonableness of answers using mental computation and estimation strategies (4.OA.3).

Develop strategies to determine the area and perimeter of rectangles in real world situations (4.MD.3).

3.NBT.2 (Prior Grade Standard)

Fluently add and subtract within 1,000 using strategies and algorithms^G based on place value, properties of operations, and/or the relationship between addition and subtraction

5.NBT.5 (Future Grade Standard)

Fluently^G multiply multi-digit whole numbers using a standard algorithm.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

<div style="border: 1px solid black; border-radius: 15px; padding: 5px; display: inline-block; margin-bottom: 10px;"> 4.NBT.5 </div> <p>Multiply a whole number of up to four digits by a one-digit whole number, and multiply two two-digit numbers, using strategies based on place value and the properties of operations. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.</p>	<p style="text-align: center;">Common Misconceptions</p> <p>Often students mix up when to 'carry' and when to 'borrow'. Also students often do not understand why they need to “borrow” and just subtract the smaller digit from the larger one. Emphasize place value and the meaning of each of the digits.</p>	<p style="text-align: center;">Academic Vocabulary/ Language</p> <ul style="list-style-type: none"> ▪ multiply ▪ equation ▪ area model ▪ rectangular arrays ▪ product <p style="text-align: center;">Tier 2</p> <ul style="list-style-type: none"> ▪ illustrate ▪ explain
<p style="text-align: center;">Essential Understandings</p> <ul style="list-style-type: none"> • The product is the result of multiplication. • Factors are the numbers being multiplied together. • There is a relationship between multiplication and division. 		
<p>Learning Targets</p>	<p>I can use and explain how to do arithmetic with multi-digit numbers.</p> <p>I can multiply a whole number up to four digits by a one-digit whole number.</p> <p>I can multiply a two-digit number by a two-digit number using strategies based on place value and/or operation properties.</p> <p>I can explain 2-digit by 2-digit multiplication by using equations, rectangular arrays, and/or area models.</p>	

Classroom Snapshot

Examples

Explain two ways to multiply 23×15 .

Solve. $3,008 \times 15$

Questions

Draw an area model that shows the problem 23×15 .

$406 \times 7 = ?$

Draw three different arrays that would model the product of 24.

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

As students developed an understanding of multiplying a whole number up to four digits by a one-digit whole number, and multiplying two two-digit numbers through various strategies, they should do the same when finding whole-number quotients and remainders. By relating division to multiplication and repeated subtraction, students can find partial quotients. An explanation of partial quotients or this video can be viewed at <http://www.teachertube.com>, search for Outline of Partial Quotients. This strategy will help them understand the division algorithm. Students will have a better understanding of multiplication or division when problems are presented in context. Students should be able to illustrate and explain multiplication and division calculations by using equations, rectangular arrays and the properties of operations. These strategies were used in Grade 3 as students developed an understanding of multiplication. To give students an opportunity to communicate their understandings of various strategies, organize them into small groups and ask each group to create a poster to explain a particular strategy and then present it to the class. Students should have an understanding of terms such as sum, difference, fewer, more, less, ones, tens, hundreds, thousands, digit, whole numbers, product, factors and multiples.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Multiply or divide to solve word problems involving multiplicative comparisons (4.OA.2).

Solve multi-step word problems with whole numbers and assess the reasonableness of answers using mental computation and estimation strategies (4.OA.3).

Develop strategies to determine the area and perimeter of rectangles in real world situations (4.MD.3).

3.NBT.3 (Prior Grade Standard)

Multiply one-digit whole numbers by multiples of 10 in the range 10-90, e.g., 9×80 , 5×60 using strategies based on place value and properties of operations.

5.NBT.5 (Future Grade Standard)

Fluently ^G multiply multi-digit whole numbers using a standard algorithm.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.NBT.6

Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.

Essential Understandings

- There are two major division situations: fair sharing (group size unknown) and repeated subtraction (number of groups unknown). See Table 2, page 96.
- There is a relationship between multiplication and division.
- The dividend divided by the divisor is the quotient.
- A remainder can be stated, can be discarded, or can force the quotient to increase to the next whole number depending on the context.
- Equations, rectangular arrays, and/or area models can be used to illustrate and explain multiplication and division.

Common Misconceptions

When working with division, students often do not think about the importance of place value. They treat each digit in the dividend separately without looking at the value of the entire number.

Encourage students to explore different strategies and consider the relationship between multiplication and division. Estimating by using multiplication prior to dividing, helps students see what a reasonable quotient will be.

**Academic Vocabulary/
Language**

- quotient
- remainder
- dividend
- divisor

Tier 2

- illustrate
- explain

Learning Target

I can use and explain how to do arithmetic with multi-digit numbers.
 I can divide a single digit into numbers up to 1,000,000 in a variety of ways.
 I can show and explain these division problems by using equations, rectangular arrays, and/or area models.

Classroom Snapshot

Examples

Explain how knowing $4 \times 23 = 92$ and $4 \times 50 = 200$ would allow you to more easily solve the problem $292 \div 4$.

Explain why solving 354×5 is more easily solved by breaking the problem into $300 \times 5 + 50 \times 5 + 5 \times 5$.

Questions

Divide 584 by 4 in two different ways.

Draw and explain an area model for $426 \div 4$.

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

As students developed an understanding of multiplying a whole number up to four digits by a one-digit whole number, and multiplying two two-digit numbers through various strategies, they should do the same when finding whole-number quotients and remainders. By relating division to multiplication and repeated subtraction, students can find partial quotients. An explanation of partial quotients or this video can be viewed at <http://www.teachertube.com>, search for Outline of Partial Quotients. This strategy will help them understand the division algorithm. Students will have a better understanding of multiplication or division when problems are presented in context. Students should be able to illustrate and explain multiplication and division calculations by using equations, rectangular arrays and the properties of operations. These strategies were used in Grade 3 as students developed an understanding of multiplication. To give students an opportunity to communicate their understandings of various strategies, organize them into small groups and ask each group to create a poster to explain a particular strategy and then present it to the class. Vocabulary is important. Students should have an understanding of terms such as, sum, difference, fewer, more, less, ones, tens, hundreds, thousands, digit, whole numbers, product, factors and multiples.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Multiply or divide to solve word problems involving multiplicative comparisons (4.OA.2).

Solve multi-step word problems with whole numbers and assess the reasonableness of answers using mental computation and estimation strategies (4.OA.3).

Develop strategies to determine the area and perimeter of rectangles in real world situations (4.MD.3).

3.NBT.3 (Prior Grade Standard)

Multiply one-digit whole numbers by multiples of 10 in the range 10–90 (e.g., 9×80 , 5×60) using strategies based on place value and properties of operations.

5.NBT.6 (Future Grade Standard)

Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.NF.1

Explain why a fraction a/b is equivalent to a fraction $(n \times a)/(n \times b)$ by using visual fraction models, with attention to how the number and size of the parts differ even though the two fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

Essential Understandings

- Extend understanding of fraction equivalence and ordering limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12 and 100.
- Equivalent fractions use different sized fractional parts to describe the same amount, e.g., $1/2 = 2/4$.
- Multiplying the numerator and the denominator by the same number will result in an equivalent fraction.
- There is a multiplicative relationship between the number of equal parts in a whole and the size of the parts.

Common Misconceptions

Students think that when generating equivalent fractions they need to multiply or divide either the numerator or denominator, such as, changing $1/2$ to sixths. They would multiply the denominator by 3 to get $1/6$, instead of multiplying the numerator by 3 also. Their focus is only on the multiple of the denominator, not the whole fraction. Students need to first use a visual model then use a numeric form of the fraction one such as $3/3$ so that the numerator and denominator do not contain the original numerator or denominator.

Academic Vocabulary/ Language

- fractions
- equivalent
- fraction model

Tier 2

- explain
- recognize
- generate

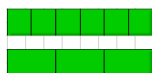
Learning Targets

- I can order fractions and explain when they are equivalent.
- I can create and explain equivalent fractions using visual models.
- I can create and explain equivalent fractions.

Classroom Snapshot

Example

Explain how this model shows that $1/3 = 2/6$



Questions

Draw a picture to show that $3/4$ and $6/8$ are equivalent fractions.

Write 5 fractions that are equivalent to $3/5$.

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Students' initial experience with fractions began in Grade 3. They used models such as number lines to locate unit fractions, and fraction bars or strips, area or length models, and Venn diagrams to recognize and generate equivalent fractions and make comparisons of fractions. Students extend their understanding of unit fractions to compare two fractions with different numerators and different denominators. Students should use models to compare two fractions with different denominators by creating common denominators or numerators. The models should be the same (both fractions shown using fraction bars or both fractions using circular models) so that the models represent the same whole. The models should be represented in drawings. Students should also use benchmark fractions such as $1/2$ to compare two fractions. The result of the comparisons should be recorded using $>$, $<$ and $=$ symbols. Students should revisit the identity property of multiplication (any number multiplied by one is itself) to understand why you can multiply a fraction by n/n to create an equivalent fraction.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Gain familiarity with factors and multiples (4.OA.4).

3.NF.3d (Prior Grade Standard)

Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size.
d. Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual fraction model.

5.NF.1-2 (Future Grade Standard)

1. Add and subtract fractions with unlike denominators (including mixed numbers and fractions greater than 1) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators. *For example, use visual models and properties of operations to show $2/3 + 5/4 = 8/12 + 15/12 = 23/12$. (In general, $a/b + c/d = (a/b \times d/d) + (c/d \times b/b) = (ad + bc)/bd$.)*
2. Solve word problems involving addition and subtraction of fractions referring to the same whole, including cases of unlike denominators, e.g., by using visual fraction models or equations to represent the problem. Use benchmark fractions and number sense of fractions to estimate mentally and assess the reasonableness of answers. *For example, recognize an incorrect result $2/5 + 1/2 = 3/7$, by observing that $3/7 < 1/2$.*



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.NF.2

Compare two fractions with different numerators and different denominators, e.g., by creating common denominators or numerators, or by comparing to a benchmark

fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual fraction model.

Essential Understanding

- Extend understanding of fraction equivalence and ordering limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12 and 100.
- Visual models, such as rectangular area models, arrays (e.g., egg cartons) and length models (including fraction strips and number lines), can be used to represent and compare fractions.
- To compare fractions using models, each fraction should be represented with the same visual model and the same sized whole.
- Multiplying the numerator and the denominator by the same number will result in an equivalent fraction.

Common Misconceptions

Students think that when generating equivalent fractions they need to multiply or divide either the numerator or denominator, such as, changing $\frac{1}{2}$ to sixths. They would multiply the denominator by 3 to get $\frac{1}{6}$, instead of multiplying the numerator by 3 also. Their focus is only on the multiple of the denominator, not the whole fraction. Students need to first use a visual model then use a numeric form of the fraction one such as $\frac{3}{3}$ so that the numerator and denominator do not contain the original numerator or denominator.

Academic Vocabulary/ Language

- fractions
- equivalent
- numerator
- denominator
- visual fraction model
- $>$, $<$, $=$

Tier 2

- compare
- create
- recognize
- valid
- record

Learning Targets

- I can order fractions and explain when they are equivalent.
- I can compare two fractions by creating common numerators or common denominators.
- I can compare two fractions using a benchmark fraction.
- I can explain why fraction comparisons are only valid when they refer to the same whole.
- I can correctly record the comparison of fractions using $<$, $>$, $=$ and I can defend my answers.

Classroom Snapshot

Examples

Find the larger fraction between $3/5$ and $3/7$.

Find the larger fraction between $5/8$ and $3/7$ by comparing each to $1/2$.

Put the following fractions in order from smallest to largest.
 $4/5, 3/4, 5/8, 7/10$

Questions

Paul's Pizza sells a $1/2$ pizza that feeds 3. Patty's Pizza says that half of their pizza only feeds one person. How is this possible?

Write the expression showing $3/8$ is smaller than $3/5$ and explain why.

Draw a model that shows why $3/5 < 3/4$.

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Students' initial experience with fractions began in Grade 3. They used models such as number lines to locate unit fractions, and fraction bars or strips, area or length models, and Venn diagrams to recognize and generate equivalent fractions and make comparisons of fractions. Students extend their understanding of unit fractions to compare two fractions with different numerators and different denominators. Students should use models to compare two fractions with different denominators by creating common denominators or numerators. The models should be the same (both fractions shown using fraction bars or both fractions using circular models) so that the models represent the same whole. The models should be represented in drawings. Students should also use benchmark fractions such as $1/2$ to compare two fractions. The result of the comparisons should be recorded using $>$, $<$ and $=$ symbols.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Gain familiarity with factors and multiples (4.OA.4).

3.NF.3 (Prior Grade Standard)

Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size.

- Understand two fractions as equivalent (equal) if they are the same size, or the same point on a number line.
- Recognize and generate simple equivalent fractions, e.g., $1/2 = 2/4$, $4/6 = 2/3$. Explain why the fractions are equivalent, e.g., by using a visual fraction model.
- Express whole numbers as fractions, and recognize fractions that are

5.NF.1-2 (Future Grade Standard)

- Add and subtract fractions with unlike denominators (including mixed numbers and fractions greater than 1) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators.
For example, use visual models and properties of operations to show $2/3 + 5/4 = 8/12 + 15/12 = 23/12$. (In general, $a/b + c/d = (a/b \times d/d) + (c/d \times b/b) = (ad + bc)/bd$.)

equivalent to whole numbers.

Examples: Express 3 in the form $3 = 3/1$; recognize that $6/1 = 6$; locate $4/4$ and 1 at the same point of a number line diagram.

d. Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual fraction model.

2. Solve word problems involving addition and subtraction of fractions referring to the same whole, including cases of unlike denominators, e.g., by using visual fraction models or equations to represent the problem. Use benchmark fractions and number sense of fractions to estimate mentally and assess the reasonableness of answers.

For example, recognize an incorrect result $2/5 + 1/2 = 3/7$, by observing that $3/7 < 1/2$.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.NF.3

Understand a fraction a/b with $a > 1$ as a sum of fractions $1/b$.

- a. Understand addition and subtraction of fractions as joining and separating parts referring to the same whole.
- b. Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model ^G.
Examples: $3/8 = 1/8 + 1/8 + 1/8$; $3/8 = 1/8 + 2/8$; $2\ 1/8 = 1 + 1 + 1/8 = 8/8 + 8/8 + 1/8$.
- c. Add and subtract mixed numbers with like denominators, e.g., by replacing each mixed number with an equivalent fraction, and/or by using properties of operations and the relationship between addition and subtraction.
- d. Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators, e.g., by using visual fraction models and equations to represent the problem.

Essential Understanding

- Fractions can be added and subtracted when the wholes are the same size.
- Unit fractions can be combined from multiple wholes if all the wholes are the same size.
- Fractions with the same denominators can be added and subtracted using visual models, properties of operations, and relationships of addition and subtraction of whole numbers.
- Mixed numbers can be written as fractions, e.g., $14/3 = 4\ 2/3$, and can be added or subtracted in this form.

Common Misconceptions

Students think that it does not matter which model to use when finding the sum or difference of fractions. They may represent one fraction with a rectangle and the other fraction with a circle. They need to know that the models need to represent the same whole.

Academic Vocabulary/

Language

- fractions
- equivalent
- numerator
- denominator
- decompose
- ordering
- mixed number

Tier 2

- solve
- represent

<ul style="list-style-type: none"> Equivalent fractions can be used to add and subtract fractions. (Fractions need not be simplified.) 		
<p>Learning Targets</p>	<p>I can use and explain unit fractions and relate what I know about arithmetic of whole numbers to the arithmetic of unit fractions.</p> <p>I can explain the concepts of adding and subtracting fractions with like denominators.</p> <p>I can decompose (break down) a fraction into a sum of fractions with the same denominator in more than one way.</p> <p>I can decompose (break down) a fraction into a sum of fractions with the same denominator and justify my answer using a visual fraction model.</p> <p>I can add mixed numbers with like denominators using a variety of strategies.</p> <p>I can subtract mixed numbers with like denominators using a variety of strategies.</p> <p>I can solve real-world problems involving addition of fractions.</p> <p>I can solve real-world problems involving subtraction of fractions.</p>	

Classroom Snapshot

<p style="text-align: center;">Example</p> <p>Use fraction bars to show the combined distance of $2\frac{3}{8}$ and $3\frac{1}{8}$.</p> <p>Explain why $5\frac{4}{6}$ is the same as $3\frac{2}{6} + 2\frac{2}{6}$.</p>	<p style="text-align: center;">Questions</p> <p>Bob walked $2\frac{3}{8}$ miles and Sue walked $3\frac{1}{8}$ miles. What is the difference in their distances? How far did they walk together?</p> <p>Draw two fraction models to show the difference between between $2\frac{3}{8}$ and $3\frac{1}{8}$.</p>
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Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

In Grade 3, students represented whole numbers as fractions. In Grade 4, they will use this knowledge to add and subtract mixed numbers with like denominators using properties of number and appropriate fraction models. It is important to stress that whichever model is used, it should be the same for the same whole. For example, a circular model and a rectangular model should not be used in the same problem. Understanding of multiplication of whole numbers is extended to multiplying a fraction by a whole number. Allow students to use fraction models and drawing to show their understanding. Present word problems involving multiplication of a fraction by a whole number. Have students solve the problems using visual models and write equations to represent the problems.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Interpret and represent multiplicative comparisons (4.OA.1).

Determine whether a whole number is a multiple on another whole number (4.OA.4).

3.NF.3b (Prior Grade Standard)

Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size.

b. Recognize and generate simple equivalent fractions, e.g., $1/2 = 2/4$, $4/6 = 2/3$. Explain why the fractions are equivalent, e.g., by using a visual fraction model.

5.NF.1-2 (Future Grade Standard)

1. Add and subtract fractions with unlike denominators (including mixed numbers and fractions greater than 1) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators.

For example, use visual models and properties of operations to show $2/3 + 5/4 = 8/12 + 15/12 = 23/12$. (In general, $a/b + c/d = (a/b \times d/d) + (c/d \times b/b) = (ad + bc)/bd$.)

2. Solve word problems involving addition and subtraction of fractions referring to the same whole, including cases of unlike denominators, e.g., by using visual fraction models or equations to represent the problem. Use benchmark fractions and number sense of fractions to estimate mentally and assess the reasonableness of answers.

For example, recognize an incorrect result $2/5 + 1/2 = 3/7$, by observing that $3/7 < 1/2$.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.NF.4

Apply and extend previous understandings of multiplication to multiply a fraction by a whole number.

- Understand a fraction a/b as a multiple of $1/b$. For example, use a visual fraction model to represent $5/4$ as the product of $5 \times (1/4)$, recording the conclusion by the equation $5/4 = 5 \times (1/4)$ or $5/4 = 1/4 + 1/4 + 1/4 + 1/4 + 1/4$.
- Understand a multiple of a/b as a multiple of $1/b$, and use this understanding to multiply a fraction by a whole number. For example, use a visual fraction model to express $3 \times (2/5)$ as $6 \times (1/5)$, recognizing this product as $6/5$. (In general, $n \times (a/b) = (n \times a)/b$.)
- Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual fraction models and equations to represent the problem. For example, if each person at a party will eat $3/8$ of a pound of roast beef, and there will be 5 people at the party, how many pounds of roast beef will be needed? Between what two whole numbers does your answer lie?

Essential Understanding

- Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12, and 100 (Fractions need not be simplified).
- Multiplication is repeated addition, i.e., just as $4 \times 3 = 3 + 3 + 3 + 3$, $5 \times 18 = 18 + 18 + 18 + 18 + 18$ which equals 58.

Common Misconceptions

Students think that it does not matter which model to use when finding the sum or difference of fractions. They may represent one fraction with a rectangle and the other fraction with a circle. They need to know that the models need to represent the same whole.

Academic Vocabulary/ Language

- fractions
- whole number
- multiple
- fraction model

Tier 2

- apply
- extend
- solve
- represent

Learning Targets	<p>I can use and explain unit fractions and relate what I know about arithmetic of whole numbers to the arithmetic of unit fractions.</p> <p>I can explain how a fraction a/b is a multiple of $1/b$.</p> <p>I can explain how multiplying a whole number times a fraction can be changed to a whole number times a unit fraction.</p> <p>I can use a visual fraction model to justify multiplying a fraction by a whole number.</p> <p>I can solve word problems involving multiplication of a fraction by a whole number using visual fraction models and equations.</p>
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Classroom Snapshot

Examples

Explain how many fourths are in $5/4$ and write an equation that shows that relationship.

If each person at a party will eat $3/8$ of a pound of roast beef, and there will be 5 people at the party, how many pounds of roast beef will be needed? Show your answer using fraction models or drawings.

Questions

What number should go in the blank? $1/6 \times \underline{\quad} = 7/6$

If the fraction bar below represents $2/5$, then what would three of these bars represent?



Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Understanding of multiplication of whole numbers is extended to multiplying a fraction by a whole number. Allow students to use fraction models and drawing to show their understanding. Present word problems involving multiplication of a fraction by a whole number. Have students solve the problems using visual models and write equations to represent the problems.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Interpret and represent multiplicative comparisons (4.OA.1).

Determine whether a whole number is a multiple on another whole number (4.OA.4).

3.NF.3 (Prior Grade Standard)

Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size.

- a. Understand two fractions as equivalent (equal) if they are the same size, or the same point on a number line.
- b. Recognize and generate simple equivalent fractions, e.g., $1/2 = 2/4$, $4/6 = 2/3$. Explain why the fractions are equivalent, e.g., by using a visual fraction model.^G
- c. Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers.

Examples: Express 3 in the form $3 = 3/1$; recognize that $6/1 = 6$; locate $4/4$ and 1 at the same point of a number line diagram.

- d. Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual fraction model.

5.NF.4 (Future Grade Standard)

4. Apply and extend previous understandings of multiplication to multiply a fraction or whole number by a fraction.

- a. Interpret the product $(a/b) \times q$ as a parts of a partition of q into b equal parts, equivalently, as the result of a sequence of operations $a \times q \div b$. For example, use a visual fraction model to show $(2/3) \times 4 = 8/3$, and create a story context for this equation. Do the same with $(2/3) \times (4/5) = 8/15$. (In general, $(a/b) \times (c/d) = ac/bd$.)

- b. Find the area of a rectangle with fractional side lengths by tiling it with unit squares of the appropriate unit fraction side lengths, and show that the area is the same as would be found by multiplying the side lengths. Multiply fractional side lengths to find areas of rectangles, and represent fraction products as rectangular areas.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.NF.5

Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10

and 100. For example, express $\frac{3}{10}$ as $\frac{30}{100}$, and add $\frac{3}{10} + \frac{4}{100} = \frac{34}{100}$. In general students who can generate equivalent fractions can develop strategies for adding fractions with unlike denominators, but addition and subtraction with unlike denominators is not a requirement at this grade.

Essential Understanding

- Using equivalent fractions, any fraction with a denominator of ten can be renamed as a fraction with a denominator of 100.

Common Misconceptions

Students think that it does not matter which model to use when finding the sum or difference of fractions. They may represent one fraction with a rectangle and the other fraction with a circle. They need to know that the models need to represent the same whole.

Academic Vocabulary/ Language

- fractions
- whole number
- multiple
- equivalent fraction
- denominator

Tier 2

- express
- respective

Learning Targets

I can write fractions with denominators of 10 to equal fractions with denominators of 100.
I can add two fractions with the denominators of 10 and 100.

Examples	Classroom Snapshot	Questions
<p>Explain how to change $\frac{7}{10}$ to an equal fraction with a denominator of 100.</p> <p>Explain how you could add $\frac{3}{10}$ to $\frac{4}{100}$ together.</p> <p>Adapted from Darke County Schools</p>		<p>Change $\frac{7}{10}$ to an equal fraction with a denominator of 100.</p> <p>Add $\frac{3}{10}$ to $\frac{4}{100}$.</p>
<p>Ohio Department of Education Model Curriculum Instructional Strategies and Resources</p> <p>Students' initial experience with fractions began in Grade 3. They used models such as number lines to locate unit fractions, and fraction bars or strips, area or length models, and Venn diagrams to recognize and generate equivalent fractions and make comparisons of fractions. Students extend their understanding of unit fractions to compare two fractions with different numerators and different denominators. Students should use models to compare two fractions with different denominators by creating common denominators or numerators. The models should be the same (both fractions shown using fraction bars or both fractions using circular models) so that the models represent the same whole. The models should be represented in drawings. Students should also use benchmark fractions such as $\frac{1}{2}$ to compare two fractions. The result of the comparisons should be recorded using $>$, $<$ and $=$ symbols.</p> <p>Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)</p>		
<p>Connections Across Standards</p> <p>Use units to solve measurement problems (4.MD.1-2).</p> <p>Generalize place value understanding (4.NBT.2).</p>		
<p>3.NF.3 (Prior Grade Standard)</p> <p>Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size.</p> <p>a. Understand two fractions as equivalent (equal) if they are the same size, or the same point on a number line.</p> <p>b. Recognize and generate simple equivalent fractions, e.g., $\frac{1}{2} = \frac{2}{4}$, $\frac{4}{6} = \frac{2}{3}$. Explain why the fractions are equivalent, e.g., by using a visual fraction model.</p> <p>c. Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers.</p> <p><i>Examples: Express 3 in the form $3 = \frac{3}{1}$; recognize that $\frac{6}{1} = 6$; locate $\frac{4}{4}$ and 1 at the same point of a number line diagram.</i></p> <p>d. Compare two fractions with the same numerator or the same</p>		<p>5.NF.4 (Future Grade Standard)</p> <p>Apply and extend previous understandings of multiplication to multiply a fraction or whole number by a fraction.</p> <p>a. Interpret the product $(\frac{a}{b}) \times q$ as a parts of a partition of q into b equal parts; equivalently, as the result of a sequence of operations $a \times q \div b$.</p> <p><i>For example, use a visual fraction model to show $(\frac{2}{3}) \times 4 = \frac{8}{3}$, and create a story context for this equation. Do the same with $(\frac{2}{3}) \times (\frac{4}{5}) = \frac{8}{15}$. (In general, $(\frac{a}{b}) \times (\frac{c}{d}) = \frac{ac}{bd}$.)</i></p> <p>b. Find the area of a rectangle with fractional side lengths by tiling it with unit squares of the appropriate unit fraction side lengths, and show that the area is the same as would be found by multiplying the side lengths. Multiply fractional side lengths to find areas of rectangles, and</p>

denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual fraction model.

represent fraction products as rectangular areas.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.NF.6

Use decimal notation for fractions with denominators 10 or 100. For example, rewrite 0.62 as $\frac{62}{100}$; describe a length as 0.62 meters; locate 0.62 on a number line diagram.

Common Misconceptions
 Students treat decimals as whole numbers when making comparison of two decimals. They think the longer the number, the greater the value. For example, they think that 0.03 is greater than 0.3.

**Academic Vocabulary/
 Language**

- fractions
- decimal
- number line

Tier 2

- notation
- rewrite
- describe
- locate

Essential Understandings

- The place value system of whole numbers can be expanded to represent numbers less than 1.
- A fraction with a denominator of 10 or 100 can be written using decimal notation.
- A number can be written as a fraction, e.g., $\frac{17}{100}$, or as a decimal, e.g., 0.17.
- A decimal point or horizontal bar can be used to show where the unit is located, e.g., $\frac{35}{100} = 0.35$.

Learning Targets

I can change fractions with denominators of 10 or 100 to decimals and can explain how these decimals differ in size.
 I can write a fraction with denominators of 10 or 100 as decimals.
 I can locate a decimal on a number line.

Classroom Snapshot

Examples

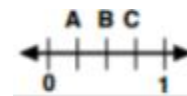
Change $32/100$ to a decimal.

Locate 0.32 on the number line.

Questions

Rewrite 0.62 as a fraction with a denominator of 100.

Which letter on the number line would represent 0.75?



Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Students' understanding of decimals to hundredths is important in preparation for performing operations with decimals to hundredths in Grade 5.

In decimal numbers, the value of each place is 10 times the value of the place to its immediate right. Students need an understanding of decimal notations before they try to do conversions in the metric system. Understanding of the decimal place value system is important prior to generalization of moving the decimal point when performing operations involving decimals.



Students extend fraction equivalence from Grade 3 with denominators of 2, 3, 4, 6 and 8 to fractions with a denominator of 10. Provide fraction models of tenth and hundredths so that students can express a fraction with a denominator of 10 as an equivalent fraction with a denominator of 100.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Use units to solve measurement problems (4.MD.1-2).

Generalize place value understanding (4.NBT.2).

3.NF.2 (Prior Grade Standard)

Understand a fraction as a number on the number line; represent fractions on a number line diagram.⁶

- a. Represent a fraction $1/b$ on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into b equal parts. Recognize that each part has size $1/b$ and that the endpoint of the part based at 0 locates the number $1/b$ on the number line.
- b. Represent a fraction a/b (which may be greater than 1) on a number line diagram by marking off a lengths $1/b$ from 0. Recognize that the resulting interval has size a/b and that its endpoint locates the number a/b on the number line.

5.NBT.2 (Future Grade Standard)

Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole number exponents to denote powers of 10.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.NF.7

Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole.

Record the results of comparisons with the symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual model.

Essential Understandings

- Decimals can only be compared when the decimals being compared refer to the same whole.
- Decimals written as tenths or hundredths can be compared using equivalent fractions

Common Misconceptions

Students treat decimals as whole numbers when making comparison of two decimals. They think the longer the number, the greater the value. For example, they think that 0.03 is greater than 0.3.

Academic Vocabulary/ Language

- fractions
- decimal
- $<$, $>$, $=$

Tier 2

- compare
- justify
- conclusion
- symbol

Learning Targets

I can compare two decimals, explain my reasoning, and record the results using $<$, $>$, or $=$.
I can explain that comparisons between two decimals are only valid when they refer to the same whole.

Classroom Snapshot

Example

Explain how you could determine which is larger, 0.45 or 0.51.

Explain why .4 is greater than .04.

Question

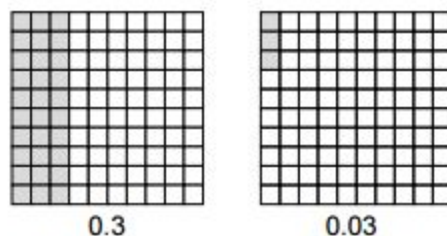
Which symbol, ($<$, $>$, $=$) should be put into the blank to make the expression true? 0.45 ____ 0.51

Khalid made a model to represent .25 and Aubrey made a model to represent .75. Whose model represents the bigger decimal? Why?

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

When comparing two decimals, remind students that as in comparing two fractions, the decimals need to refer to the same whole. Allow students to use visual models to compare two decimals. They can shade in a representation of each decimal on a 10×10 grid. The 10×10 grid is defined as one whole. The decimal must relate to the whole.



Flexibility with converting fractions to decimals and decimals to fractions provides efficiency in solving problems involving all four operations in later grades.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Use units to solve measurement problems (4.MD.1-2).

Generalize place value understanding (4.NBT.2).

3.NF.3d (Prior Grade Standard)

Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size.

d. Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual fraction model.

5.NBT.3 (Future Grade Standard)

Read, write, and compare decimals to thousandths.

a. Read and write decimals to thousandths using base-ten numerals, number names, and expanded form, e.g., $347.392 = 3 \times 100 + 4 \times 10 + 7 \times 1 + 3 \times (1/10) + 9 \times (1/100) + 2 \times (1/1000)$.

b. Compare two decimals to thousandths based on meanings of the digits in each place, using $>$, $=$, and $<$ symbols to record the results of comparisons.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.MD.1

Know relative sizes of the metric measurement units within one system of units. Metric units include kilometer, meter, centimeter, and millimeter; kilogram and gram; and liter and milliliter. Express a larger measurement unit in terms of a smaller unit. Record measurement conversions in a two-column table. For example, express the length of a 4-meter rope in centimeters. Because 1 meter is 100 times as long as a 1 centimeter, a two-column table of meters and centimeters includes the number pairs 1 and 100, 2 and 200, 3 and 300,...

Essential Understandings

- Larger units can be expressed in terms of smaller units.
- The number of units used to measure an object will depend on the size of the unit of measure.
- The larger the unit, the smaller the measurement reads; the smaller the unit, the larger the measurement reads.
- Metric units are related by powers of ten.
 - 1 kilometer = 1,000 meters, 1 meter = 100 centimeters, 1 centimeter = 10 millimeters;
 - 1 kilogram = 1,000 grams; and
 - 1 liter = 1,000 milliliters.

Common Misconceptions

Students believe that larger units will give a larger measure. Students should be given multiple opportunities to measure the same object with different measuring units. For example, have the students measure the length of a room with centimeter cubes, with centimeter rulers, and with meter sticks. Students should notice that it takes fewer meter sticks to measure the room than rulers or cubes.

Academic Vocabulary/

Language

Metric System

- kilometer
- meter
- centimeter
- millimeter
- gram
- kilogram
- milliliter
- liter

Tier 2

- relative size
- record

Learning Targets

I can explain the relative sizes of units within the metric system.
 I can translate the larger units into equivalent smaller units.
 I can record measurement equivalence in a two column table or as number pairs.

Classroom Snapshot

Examples

Explain how a kilometer, a meter and a centimeter are different.

Explain how to change a kilogram into a gram.

Questions

How many meters long is a whale that measures 300 centimeters?

How many times heavier is a gram than a kilogram?

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

In order for students to have a better understanding of the relationships between units, they need to use measuring devices in class. The number of units needs to relate to the size of the unit. Allow students to use meter sticks and rulers marked with centimeters to discover the relationship between centimeters and meters.. Have students record the relationships in a two column table or t-charts.

Career Connection

Students will use meter sticks and rulers with centimeters to solve problems with different units. Host a career speaker in the classroom to discuss how measurement and various units are used across their career field (e.g., construction, carpentry, design). Consider inviting a speaker who works on a school-based project, at your school or nearby, to share information about their work on school campuses. Lead a discussion that allows students to reflect on their work with different units and how it applies to the careers shared in the speaker's presentation.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Generalize place value understanding for multi-digit whole numbers (4.NBT.1 - 2).

Use place value operations and properties of operations to perform multi-digit arithmetic (4.NBT.5).

Use the four operations with whole numbers to solve problems (4.OA.2 – 3).

Build fractions from unit fractions (4.NF.3-4).

Understand decimal notation for fractions, and compare decimal fractions (4.NF.5 – 7).

3.MD.2 (Prior Grade Standard)

Measure and estimate liquid volumes and masses of objects using standard units of grams, kilograms, and liters. Add, subtract, multiply, or divide whole numbers to solve one-step word problems involving masses or volumes that are given in the same units, e.g., by using drawings (such as a beaker with a measurement scale) to represent the problem. Excludes multiplicative comparison problems involving notions of "times as much"; see Glossary, Table 2.

5.MD.1 (Future Grade Standard)

Know relative sizes of these U.S. customary measurement units: pounds, ounces, miles, yards, feet, inches, gallons, quarts, pints, cups, fluid ounces, hours, minutes, and seconds. Convert between pounds and ounces; miles and feet; yards, feet, and inches; gallons, quarts, pints, cups, and fluid ounces; hours, minutes, and seconds in solving multi-step, real-world problems.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.MD.2

Solve real-world problems involving money, time, and metric measurement.

- a. Using models, add and subtract money and express the answer in decimal notation.
- b. Using number line diagrams ^G, clocks, or other models, add and subtract intervals of time in hours and minutes.
- c. Add, subtract, and multiply whole numbers to solve metric measurement problems involving distances, liquid volumes, and masses of objects.

Essential Understandings

- Solve problems involving measurement.
- Answers to money problems can include the dollar symbol, \$, and decimal point placed appropriately in decimal notation.
- Answers to time problems should include a.m. and p.m. as appropriate.

Common Misconceptions

Students believe that larger units will give the larger measure. Students should be given multiple opportunities to measure the same object with different measuring units. For example, have the students measure the length of a room with centimeter cubes, with rulers marked with centimeters, and with meter sticks. Students should notice that it takes fewer meter sticks to measure the room than rulers or tiles.

Academic Vocabulary/ Language

- interval
- decimal notation
- line diagrams
- hours
- minutes
- liquid volume
- mass

Metric System

- kilometer
- meter
- centimeter
- millimeter
- gram
- kilogram
- milliliter
- liter

Tier 2

- relative size
- record

Learning Targets

I can use a model to add and subtract money and express my answer in a decimal notation.
 I can use number line diagrams, clocks, or other models to add and subtract intervals of time in hours and minutes.
 I can add, subtract, and multiply whole numbers to solve metric measurement problems involving distances, liquid volumes, and masses of objects.

Classroom Snapshot

Examples

Jill bought some school supplies. She bought a notebook for \$1.15, markers for \$2.25 and a new eraser for \$0.95. How much did Jill spend on school supplies in all? Explain.

bottle?

Brendan did chores on Saturday. He mowed the lawn for 2 hours and 15 minutes, cleaned his bedroom for 40 minutes and cleaned the garage for 1 hour and 25 minutes. How much time did Brendan do chores on Saturday? Explain.

Adapted from Darke County Schools

Questions

Mary wants to divide 1 liter of soda between 12 party cups. How many milliliters will each cup contain?

How many cups holding 150 milliliters will it take to fill a 2 liter

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Students are to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving **simple fractions or decimals**, and problems that require expressing measurements given in a larger unit in terms of a smaller unit.

Career Connection

Students will use meter sticks and rulers with centimeters to solve problems with different units. Host a career speaker in the classroom to discuss how measurement and various units are used across their career field (e.g., construction, carpentry, design). Consider inviting a speaker who works on a school-based project, at your school or nearby, to share information about their work on school campuses. Lead a discussion that allows students to reflect on their work with different units and how it applies to the careers shared in the speaker's presentation.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Generalize place value understanding for multi-digit whole numbers (4.NBT.1 - 2).

Use place value operations and properties of operations to perform multi-digit arithmetic (4.NBT.5).

Use the four operations with whole numbers to solve problems (4.OA.2 - 3).

Understand decimal notation for fractions, and compare decimal fractions (4.NF.5 - 7).

3.MD.1-2 (Prior Grade Standard)

1. Work with time and money.
 - a. Tell and write time to the nearest minute. Measure time intervals in minutes (within 90 minutes). Solve real-world problems involving addition and subtraction of time intervals (elapsed time) in minutes, e.g., by representing the problem on a number line diagram or clock.
 - b. Solve word problems by adding and subtracting within 1,000, dollars with dollars and cents with cents (not using dollars and cents simultaneously) using the \$ and ¢ symbol appropriately (not including decimal notation).
2. Measure and estimate liquid volumes and masses of objects using standard units of grams, kilograms, and liters. Add, subtract, multiply, or divide whole numbers to solve one-step word problems involving masses or volumes that are given in the same units, e.g., by using drawings (such as a beaker with a measurement scale) to represent the problem. Excludes multiplicative comparison problems involving notions of "times as much"; Table 2, page 96.

5.MD.1 (Future Grade Standard)

Know relative sizes of these U.S. customary measurement units: pounds, ounces, miles, yards, feet, inches, gallons, quarts, pints, cups, fluid ounces, hours, minutes, and seconds. Convert between pounds and ounces; miles and feet; yards, feet, and inches; gallons, quarts, pints, cups, and fluid ounces; hours, minutes, and seconds in solving multi-step, real-world problems.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

<div style="border: 1px solid black; border-radius: 15px; padding: 10px; display: inline-block; margin-bottom: 10px;"> 4.MD.3 </div> <p>Develop efficient strategies to determine the area and perimeter of rectangles in real-world situations and mathematical problems. <i>For example, given the total area and one side length of a rectangle, solve for the unknown factor, and given two adjacent side lengths of a rectangle, find the perimeter.</i></p>	<p>Common Misconceptions Students believe that larger units will give the larger measure. Students should be given multiple opportunities to measure the same object with different measuring units. For example, have the students measure the length of a room with centimeter cubes, with rulers marked with centimeters, and with meter sticks. Students should notice that it takes fewer meter sticks to measure the room than rulers or tiles.</p>	<p>Academic Vocabulary/ Language</p> <ul style="list-style-type: none"> ▪ perimeter ▪ area ▪ adjacent ▪ strategy <p>Tier 2</p> <ul style="list-style-type: none"> ▪ apply ▪ solve ▪ explain
<p style="text-align: center;">Essential Understandings</p> <ul style="list-style-type: none"> • The area of a rectangle can be found by multiplying the lengths of adjacent sides (length and width) of the rectangle. • Given an area or a perimeter of a rectangle and one side length, the adjacent side length can be determined. 		
<p>Learning Targets</p>	<p>I can use efficient strategies solve real-world problems involving the perimeter of rectangles. I can use efficient strategies solve real-world problems involving the area of rectangles.</p>	

Classroom Snapshot

Examples

Draw at least three different rectangles that have a perimeter of 24 feet.

Explain how to make the largest rectangular area given 24 feet of fence.

Questions

The area of the living room floor is 210 square feet. If it has a width of 14 feet, what is the length?

If the perimeter of a rectangle is 50 meters and the width is 10 meters, what is the length?

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Students used models to find area and perimeter in Grade 3. They need to relate discoveries from the use of models to develop an understanding of the area and perimeter formulas to solve real-world and mathematical problems.

Career Connection

Students will use yard and meter sticks and rulers with inches and centimeters to solve problems with different units. Host a career speaker in the classroom to discuss how measurement and various units are used across their career field (e.g., construction, carpentry, design). Consider inviting a speaker who works on a school-based project, at your school or nearby, to share information about their work on school campuses. Lead a discussion that allows students to reflect on their work with different units and how it applies to the careers shared in the speaker's presentation.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Generalize place value understanding for multi-digit whole numbers (4.NBT.1 - 2).

Use place value operations and properties of operations to perform multi-digit arithmetic (4.NBT.5).

Use the four operations with whole numbers to solve problems (4.OA.2 - 3).

Understand decimal notation for fractions, and compare decimal fractions (4.NF.5 - 7).

3.MD.5-8 (Prior Grade Standard)

5. Recognize area as an attribute of plane figures and understand concepts of area measurement.

a. A square with side length 1 unit, called "a unit square," is said to have "one square unit" of area, and can be used to measure area.

b. A plane figure which can be covered without gaps or overlaps by n unit squares is said to have an area of n square units.

6. Measure areas by counting unit squares (square cm, square m, square in, square ft, and improvised units).

7. Relate area to the operations of multiplication and addition.

5.MD.5 (Future Grade Standard)

Relate volume to the operations of multiplication and addition and solve real-world and mathematical problems involving volume.

a. Find the volume of a right rectangular prism with whole-number side lengths by packing it with unit cubes, and show that the volume is the same as would be found by multiplying the edge lengths, equivalently by multiplying the height by the area of the base. Represent threefold whole-number products as volumes, e.g., to represent the Associative Property of Multiplication.

b. Apply the formulas $V = \ell \times w \times h$ and $V = B \times h$ for rectangular

- a. Find the area of a rectangle with whole-number side lengths by tiling it, and show that the area is the same as would be found by multiplying the side lengths.
- b. Multiply side lengths to find areas of rectangles with whole-number side lengths in the context of solving real-world and mathematical problems, and represent whole-number products as rectangular areas in mathematical reasoning.
- c. Use tiling to show in a concrete case that the area of a rectangle with whole-number side lengths a and $b + c$ is the sum of $a \times b$ and $a \times c$ (represent the distributive property with visual models including an area model).
- d. Recognize area as additive. Find the area of figures composed of rectangles by decomposing into non-overlapping rectangles and adding the areas of the non-overlapping parts, applying this technique to solve real-world problems.
8. Solve real-world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.

- prisms to find volumes of right rectangular prisms with whole number edge lengths in the context of solving real-world and mathematical problems.
- c. Recognize volume as additive. Find volumes of solid figures composed of two non-overlapping right rectangular prisms by adding the volumes of the non-overlapping parts, applying this technique to solve real-world problems.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.MD.4

Display and interpret data in graphs (picture graphs, bar graphs, and line plots ^G) to solve problems using numbers and operations for this grade.

Essential Understandings

- Data can be organized and represented in a picture graph, a bar graph, or a line plot.
- The key of a picture graph tells how many items each picture or symbol represents.
- The scale of a line plot can be whole numbers, halves, quarters, tenths, or hundredths.
- The scale of a bar graph varies depending on the data set.
- Symbols used in picture graphs and line plots should be consistently spaced and sized for visual accuracy.
- Information presented in a graph can be used to solve problems involving the data in the graph.

Common Misconceptions

Students may not choose the correct interval for when they create a bar graph or may not choose the right value of each symbol in their picture graph. Students need experiences with a variety of data so they can choose the interval that helps to display the data clearly.

Students may choose to display non numerical data in a line plot, for example “Favorite Pizza Toppings”.

Academic Vocabulary/

Language

- line plot
- bar graph
- picture graph
- interpret
- data

Tier 2

- solve
- represent

Learning Targets

- I can use information from a line plot to solve problems using numbers and operations.
- I can use information from a picture graph to solve problems using numbers and operations.
- I can use information from a bar graph to solve problems using numbers and operations.

Classroom Snapshot

Examples

Create a line plot from the measurement of the length of student pencils in the classroom to the nearest centimeter

Create a picture graph from the following data:



Questions

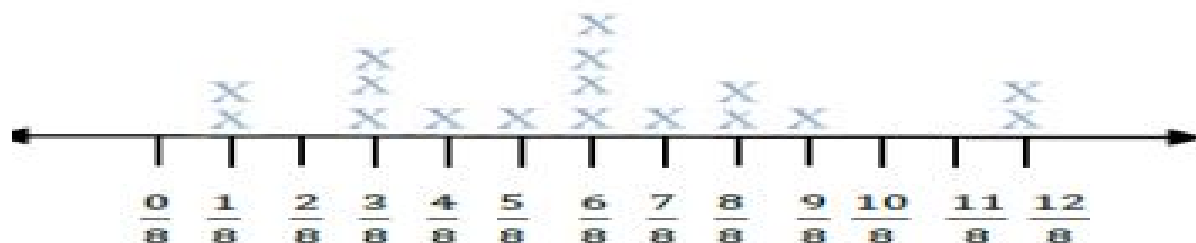
What is the difference in length between the most common length of students' pencils and the shortest length of students' pencils?

In Mrs. Rensel's class, 12 kids have a dog, 8 kids have a cat, 0 kids have a fish and 4 kids have a hamster. Create a bar graph to display this data about their class pets.

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Data has been measured and represented on line plots in units of whole numbers, halves or quarters. Students have also represented fractions on number lines. Now students are using line plots to display measurement data in fraction units and using the data to solve problems involving addition or subtraction of fractions. Have students create line plots with fractions of a unit ($\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{8}$) and plot data showing multiple data points for each fraction.



Pose questions that students may answer, such as;

- “How many one-eighths are shown on the line plot?” Expect “two one-eighths” as the answer. Then ask, “What is the total of these two one-eighths?” Encourage students to count the fractional numbers as they would with whole-number counting, but using the fraction name.
- “What is the total number of inches for insects measuring $\frac{3}{8}$ inches?”

Students can use skip counting with fraction names to find the total, such as, “three-eighths, six-eighths, nine-eighths. The last fraction names the total. Students should notice that the denominator did not change when they were saying the fraction name. Have them make a statement about the result of adding fractions with the same denominator.

Students need to be shown data in a variety of graphs (bar graphs, picture graphs and line plots) and solve problems involving the data.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Solve grade-level appropriate problems using the four operations (4.OA.1-3).
Extend the understanding of fraction equivalence and ordering (4.NF.1-2).

3.MD.3-4 (Prior Grade Standard)

3. Create scaled bar graphs to represent a data set with several categories. Solve two-step “how many more” and “how many less” problems using information presented in the scaled graphs. For example, create a bar graph in which each square in the bar graph might represent 5 pets, then determine how many more/less in two given categories.

4. Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by creating a line plot^G, where the horizontal scale is marked off in appropriate units—whole numbers, halves, or quarters.

5.MD.2 (Future Grade Standard)

Display and interpret data in graphs (picture graphs, bar graphs, and line plots^G) to solve problems using numbers and operations for this grade, e.g., including U.S. customary units in fractions $1/2$, $1/4$, $1/8$, or decimals.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.MD.5

Recognize angles as geometric shapes that are formed wherever two rays share a common endpoint, and understand concepts of angle

measurement:

- a. An angle is measured with reference to a circle with its center at the common endpoint of the rays, by considering the fraction of the circular arc between the points where the two rays intersect the circle. An angle that turns through $1/360$ of a circle is called a "one-degree angle," and can be used to measure angles.
- b. An angle that turns through n one-degree angles is said to have an angle measure of n degrees.

Essential Understandings

- Angles are formed when two rays share a common endpoint; the common endpoint of the rays is called a vertex.
- Angles are measured in degrees.
- A protractor is a tool used to measure angles.
- There are 360 degrees in a circle.
- One degree is $1/360$ of a circle.

Common Misconceptions

Students are confused as to which number to use when determining the measure of an angle using a protractor because most protractors have a double set of numbers. Students should decide first if the angle appears to be an angle that is less than the measure of a right angle (90°) or greater than the measure of a right angle (90°). If the angle appears to be less than 90° , it is an acute angle and its measure ranges from 0° to 89° . If the angle appears to be an angle that is greater than 90° , it is an obtuse angle and its measures range from 91° to 179° . Ask questions about the appearance of the angle to help students in deciding which number to use.

Academic Vocabulary/ Language

- angle
- degree
- ray
- circle
- protractor
- endpoint
- geometric shape

Tier 2

- recognize
- reference

Learning Targets

- I can draw, measure, and explain different concepts of angles.
- I can explain how an angle is made of two rays with common endpoints.
- I can explain how an angle is measured by its reference to a circle.
- I can define and explain a "one-degree angle" and how it is used to measure angles.

Classroom Snapshot

Examples

Draw and explain the parts of an angle.

Explain how to measure an angle.

Explain how many "one degree angles" it takes to be equivalent to another given angle.

Question

Which letter shows the vertex of an angle?



Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Angles are geometric shapes composed of two rays that are infinite in length. Students can understand this concept by using two rulers held together near the ends. The rulers can represent the rays of an angle. As one ruler is rotated, the size of the angle is seen to get larger. Ask questions about the types of angles created. Responses may be in terms of the relationship to right angles. Introduce angles as acute (less than the measure of a right angle) and obtuse (greater than the measure of a right angle). Have students draw representations of each type of angle. They also need to be able to identify angles in two-dimensional figures.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Draw and identify lines and angles, and classify shapes by properties of their lines and angles (4.G.1-2).

Use the four operations to solve problems (4.OA.3).

Understand fraction equivalence and ordering (4.NF.1-2).

(Prior Grade Standard)

N/A

(Future Grade Standard)

N/A



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.MD.6

Measure angles in whole-number degrees using a protractor. Sketch angles of specified measure.

Common Misconceptions

Students are confused as to which number to use when determining the measure of an angle using a protractor because most protractors have a double set of numbers. Students should decide first if the angle appears to be an angle that is less than the measure of a right angle (90°) or greater than the measure of a right angle (90°). If the angle appears to be less than 90° , it is an acute angle and its measure ranges from 0° to 89° . If the angle appears to be an angle that is greater than 90° , it is an obtuse angle and its measures range from 91° to 179° . Ask questions about the appearance of the angle to help students in deciding which number to use.

Academic Vocabulary/ Language

- angle
- degree
- protractor

Tier 2

- sketch
- draw
- explain
- specified

Essential Understandings

- Geometric measurement: understand concepts of angle and measure angles.
- A straight angle has a measurement of 180 degrees.
- A right angle has a measurement of 90 degrees.

Learning Targets

- I can draw, measure, and explain different concepts of angles.
- I can use a protractor to measure whole degree angles.
- I can draw an angle of specified size, using a protractor.

Classroom Snapshot

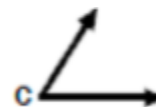
Examples

The student can use a protractor to properly measure an angle.

The student can draw an angle of a given size with a protractor.

Questions

Measure angle C.



Draw a 60 degree angle with the given protractor.

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Students are ready to use a tool to measure angles once they understand the difference between an acute angle and an obtuse angle. Angles are measured in degrees. There is a relationship between the number of degrees in an angle and circle which has a measure of 360 degrees. Students are to use a protractor to measure angles in whole-number degrees. They can determine if the measure of the angle is reasonable based on the relationship of the angle to a right angle. They also make sketches of angles of specified measure.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Draw and identify lines and angles, and classify shapes by properties of their lines and angles (4.G.1-2).

Understand fraction equivalence and ordering (4.NF.1-2).

Use the four operations to solve problems (4.OA.3).

(Prior Grade Standard)

N/A

(Future Grade Standard)

N/A



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.MD.7

Recognize angle measure as additive. When an angle is decomposed into non-overlapping parts, the angle measure of the whole is the sum of the angle measures of the parts. Solve addition and subtraction problems to find

unknown angles on a diagram in real world and mathematical problems, e.g., by using an equation with a symbol for the unknown angle measure.

Essential Understanding

- Angles can be decomposed into unit angles. (n degrees is n one degree angles.)

Common Misconceptions

Students are confused as to which number to use when determining the measure of an angle using a protractor because most protractors have a double set of numbers. Students should decide first if the angle appears to be an angle that is less than the measure of a right angle (90°) or greater than the measure of a right angle (90°). If the angle appears to be less than 90° , it is an acute angle and its measure ranges from 0° to 89° . If the angle appears to be an angle that is greater than 90° , it is an obtuse angle and its measures range from 91° to 179° . Ask questions about the appearance of the angle to help students in deciding which number to use.

Academic Vocabulary/ Language

- angle
- degree
- protractor
- additive
- decompose
- equation
- symbol
- unknown angle measure

Tier 2

- recognize
- solve
- diagram

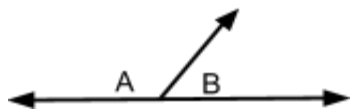
Learning Targets

I can draw, measure, and explain different concepts of angles.
I can explain how when angles are joined in non overlapping parts, the total measure is the sum of the parts.
I can solve real-world problems involving addition and/or subtraction to find unknown angles on a diagram.

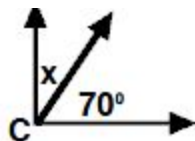
Classroom Snapshot

Examples

Explain how angle A and angle B are related in this diagram.

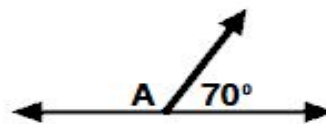


Write an equation and solve for x if angle C is a right angle.



Question

What is the measure of angle A?



Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Students are ready to use a tool to measure angles once they understand the difference between an acute angle and an obtuse angle. Angles are measured in degrees. There is a relationship between the number of degrees in an angle and circle which has a measure of 360 degrees. Students are to use a protractor to measure angles in whole-number degrees. They can determine if the measure of the angle is reasonable based on the relationship of the angle to a right angle. They also make sketches of angles of specified measure.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Draw and identify lines and angles, and classify shapes by properties of their lines and angles (4.G.1-2).

Understand fraction equivalence and ordering (4.NF.1-2).

Use the four operations to solve problems (4.OA.3).

(Prior Grade Standard)

N/A

5.MD.5c (Future Grade Standard)

Relate volume to the operations of multiplication and addition and solve real-world and mathematical problems involving volume.
c. Recognize volume as additive. Find volumes of solid figures composed of two non-overlapping right rectangular prisms by adding the volumes of the non-overlapping parts, applying this technique to solve real-world problems.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

4.G.1

Draw points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines. Identify these in two-dimensional figures.

Common Misconceptions

Students believe a wide angle with short sides may seem smaller than a narrow angle with long sides. Students can compare two angles by tracing one and placing it over the other. Students will then realize that the length of the sides does not determine whether one angle is larger or smaller than another angle. The measure of the angle does not change.

Academic Vocabulary/ Language

- right angle
- acute angle
- obtuse angle
- two –dimensional figure
- point
- perpendicular lines
- parallel lines
- line segments
- rays
- lines

Tier 2

- draw
- identify

Essential Understandings

- A point is a location in space; it has no length, width, or height.
- A line is a continuous straight path that extends indefinitely in two opposite directions.
- A line segment is a continuous straight path between two points.
- A ray is a continuous straight path that extends indefinitely in one direction from one point.
- Angles are made of two rays with the same endpoint; the endpoint is called the vertex.
- A right angle has a measure of 90° .
- An acute angle has a measure of less than 90° .
- An obtuse angle has a measure between 90° and 180°
- A plane is a flat surface that extends infinitely in all directions.

Learning Targets

- I can draw and identify lines and angles and use these to classify shapes.
- I can draw and identify a point.
- I can draw and identify a line.
- I can draw and identify a line segment.
- I can draw and identify a ray.
- I can draw and identify an acute angle.

	I can draw and identify a right angle. I can draw and identify an obtuse angle. I can draw and identify perpendicular lines. I can draw and identify parallel lines.
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Classroom Snapshot

Example

These are pretty straight forward skills of having a student properly represent a drawing of each of these and be able to identify each one. Be careful to not always orient these drawings the same each time.

Questions

Draw a line segment and a ray. Explain how they are different.

Find examples of parallel lines and perpendicular lines within the classroom.

Find examples of acute, right and obtuse angles within the classroom.

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Angles

Students can and should make geometric distinctions about angles without measuring or mentioning degrees. Angles should be classified in comparison to right angles, such as larger than, smaller than or the same size as a right angle. Students can use the corner of a sheet of paper as a benchmark for a right angle. They can use a right angle to determine relationships of other angles.

Two-dimensional shapes

Two-dimensional shapes are classified based on relationships by the angles and sides. Students can determine if the sides are parallel or perpendicular, and classify accordingly. Characteristics of rectangles (including squares) are used to develop the concept of parallel and perpendicular lines. The characteristics and understanding of parallel and perpendicular lines are used to draw rectangles. Repeated experiences in comparing and contrasting shapes enable students to gain a deeper understanding about shapes and their properties.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4 (Adjusted to reflect standards revisions.)

Connections Across Standards

Students can use recognition of angle measures to classify two-dimensional figures (4.MD.5 and 4.MD.6).

3.G.1 (Prior Grade Standard)

Draw and describe triangles, quadrilaterals (rhombuses, rectangles, and squares), and polygons (up to 8 sides) based on the number of sides and the presence or absence of square corners (right angles).

5.G.3-4 (Future Grade Standard)

3. Identify and describe commonalities and differences of triangles based on angle measures (equiangular, right, acute, and obtuse triangles) and side lengths (isosceles, equilateral, and scalene triangles).
4. Identify and describe commonalities and differences of quadrilaterals based on angle measures, side lengths, and the presence or absence of parallel and perpendicular lines, e.g., squares, rectangles, parallelograms, trapezoids^G, and rhombuses.



Ohio's Learning Standards-Clear Learning Targets

Math Grade 4

<div style="border: 1px solid black; border-radius: 15px; padding: 10px; display: inline-block;"> <h3 style="margin: 0;">4.G.2</h3> </div>	<p>Classify two-dimensional figures based on the presence or absence of parallel or perpendicular lines, or the presence or absence of angles of a specified size.</p>	<p style="text-align: center;">Common Misconceptions</p> <p>Students believe a wide angle with short sides may seem smaller than a narrow angle with long sides. Students can compare two angles by tracing one and placing it over the other. Students will then realize that the length of the sides does not determine whether one angle is larger or smaller than another angle. The measure of the angle does not change.</p>	<p style="text-align: center;">Academic Vocabulary/ Language</p> <ul style="list-style-type: none"> ▪ right angle ▪ acute angle ▪ obtuse angle ▪ two –dimensional figures ▪ perpendicular lines ▪ parallel lines <p style="text-align: center;">Tier 2</p> <ul style="list-style-type: none"> ▪ classify ▪ presence ▪ absence ▪ recognize ▪ identify
<p style="text-align: center;">Essential Understandings</p> <ul style="list-style-type: none"> • Two lines (or two line segments) in a plane are perpendicular if the angle between them is a right angle. • Two lines (or two line segments) in a plane are parallel if they do not intersect. • Two-dimensional figures can be classified (based on the presence or absence of parallel or perpendicular lines or presence or absence of angles of a specified size). 			
<p>Learning Targets</p>	<p>I can draw and identify lines and angles and use these to classify shapes. I can put 2-D figures in like groups based on whether certain sides are parallel or perpendicular. I can put 2-D figures in like groups based on whether certain angles are acute, obtuse, or right.</p>		

Classroom Snapshot

Examples

The student can group shapes based on whether the sides are parallel or perpendicular.

The student can group triangles based on whether they contain a right angle or not.

Adapted from Darke County Schools

Question

Give students an array of shapes and have the students sort them in appropriate groups. Students should be able to articulate in precise mathematical language why the groups are classified the way they are.

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Angles

Students can and should make geometric distinctions about angles without measuring or mentioning degrees. Angles should be classified in comparison to right angles, such as larger than, smaller than or the same size as a right angle. Students can use the corner of a sheet of paper as a benchmark for a right angle. They can use a right angle to determine relationships of other angles.

Two-dimensional shapes

Two-dimensional shapes are classified based on relationships by the angles and sides. Students can determine if the sides are parallel or perpendicular, and classify accordingly. Characteristics of rectangles (including squares) are used to develop the concept of parallel and perpendicular lines. The characteristics and understanding of parallel and perpendicular lines are used to draw rectangles. Repeated experiences in comparing and contrasting shapes enable students to gain a deeper understanding about shapes and their properties.

Adapted from Ohio Mathematics Model Curriculum 2015 Grade 4

Connections Across Standards

Students can use recognition of angle measures to classify two-dimensional figures (4.MD.5 and 4.MD.6).

3.G.1 (Prior Grade Standard)

Draw and describe triangles, quadrilaterals (rhombuses, rectangles, and squares), and polygons (up to 8 sides) based on the number of sides and the presence or absence of square corners (right angles).

5.G.4 (Future Grade Standard)

Identify and describe commonalities and differences of quadrilaterals based on angle measures, side lengths, and the presence or absence of parallel and perpendicular lines, e.g., squares, rectangles, parallelograms, trapezoids^G, and rhombuses.